# Design Dała 18 

## Equivalent Flow Capacity of Various Pipe Materials

Design of a non-pressure sewerage system requires selection of adequately sized pipe to carry maximum predicted flow, at a given slope, without flooding. If more than one type of pipe is considered, all pipe sizes of the various materials must have equivalent flow capacity. A comparison of pipe diameters with different surface roughness coefficients is an important design consideration.
For any given design flow and pipe slope, the Manning Formula is conveniently express as:

$$
Q=\frac{1.486}{n} \times A \times R^{2 / 3} \times S^{1 / 2}
$$

Where:
$Q=$ discharge, cubic feet per second
$S=$ Slope of pipe, feet of vertical drop
per foot of horizontal distance
$n=$ Manning's roughness coefficient
$A=$ cross-sectional area of flow,
square feet for circular pipe
flowing full $A=\frac{\pi D^{2}}{4}$
$R=$ hydraulic radius, feet (equals the
area of the flow divided by the
wetted perimeter)

For circular pipe flowing full, the hydraulic radius is equal to the area of the pipe crosssection divided by the pipe circumference:

$$
\mathrm{R}=\frac{\mathrm{A}}{\mathrm{~W} . \mathrm{P} .}=\frac{\frac{\pi \mathrm{D}^{2}}{4}}{\pi \mathrm{D}}=\frac{\mathrm{D}}{4}
$$

Substitution of the values for $A$ and $R$ in the Manning Formula results in the following:

$$
\frac{\mathrm{Q}}{\mathrm{~S}^{1 / 2}}=\frac{1.486}{n} \times \frac{\pi \mathrm{D}}{4} \times\left[\frac{\mathrm{D}}{4}\right]^{2 / 3}=\mathrm{K} \times \frac{\mathrm{D}^{8 / 3}}{n}
$$

where K is a discharge factor dependent on the ratio of the depth of flow to some other linear dimension of the cross-section. For circular pipe operating under full flow conditions, $K=0.463$.

Because design and slope are the same regardless of the sizes or types of pipe under consideration:

$$
\mathrm{K}_{\mathrm{m}, \mathrm{p}}=\frac{\mathrm{D}_{\mathrm{m}, \mathrm{p}}^{8 / 3}}{n_{\mathrm{m}, \mathrm{p}}}=\mathrm{K}_{\mathrm{c}} \frac{\mathrm{D}_{\mathrm{c}}^{8 / 3}}{n_{\mathrm{c}}}
$$

$\mathrm{K}_{\mathrm{m}, \mathrm{p}}, \mathrm{D}_{\mathrm{m}, \mathrm{p}}$ and $n_{\mathrm{m}, \mathrm{p}}$ represent the discharge factor, diameter and roughness coefficient of corrugated metal pipe and $\mathrm{K}_{\mathrm{c}}, \mathrm{D}_{\mathrm{c}}$ and $n_{c}$ represent the discharge factor, diameter and roughness coefficient of concrete and other smoothwalled pipe. The full flow value of $\mathrm{K}=$ 0.463 is the same for all circular pipe. For two different types of pipe flowing full on the same slope and designed to carry the same flow, the equation reduces to:

$$
\begin{aligned}
& \frac{\mathrm{D}_{\mathrm{m}, \mathrm{p}}^{8 / 3}}{n_{\mathrm{m}, \mathrm{p}}^{8}}=\frac{\mathrm{D}_{\mathrm{c}}^{8 / 3}}{n_{\mathrm{c}}} \\
& \mathrm{D}_{\mathrm{m}, \mathrm{p}}=\left[\frac{n_{\mathrm{m}, \mathrm{p}}}{n_{\mathrm{c}}}\right]^{3 / 8} \mathrm{D}_{\mathrm{c}}
\end{aligned}
$$

The above equation illustrates that the relative pipe sizes are dependent on the ratio of the respective roughness coefficients.

Table 1 lists recommended values for Manning's Roughness Coefficients of various materials of pipe.

Table 1 Recommended Values of Mannings $n$

| Pipe <br> Material | Values of Manning's $\boldsymbol{n}$ |  |
| :--- | :--- | :---: |
|  | Laboratory <br> Values | ACPA Recommended <br> Design Values |
| Concrete <br> Pipe | 0.010 | Storm Sewer - 0.012 <br> Sanitary Sewer-0.012-0.013 |
| Corrugated <br> HDPE <br> (lined) | $0.009-0.015$ | Storm Sewer-0.012-0.024 |
| Corrugated <br> Metal Pipe | $0.022-0.028$ | Storm Sewer-0.029-0.034 |
| Spiral Rib <br> Metal Pipe | $0.012-0.013$ | Storm Sewer-0.016-0.018 |

Results of numerous test programs conducted under laboratory conditions have shown the roughness coefficient of concrete pipe to range between 0.009 and 0.011 . The design values of 0.012 and 0.013 , shown in Table 1, have been generally used to account for the possible build up of slime or grease in sanitary sewers and foreign debris in storm sewers. Therefore, design values should also be used for the other materials shown in the table to allow for a factor of safety as seen with concrete pipe. The larger variation in Manning's " $n$ " lab values in Corrugated HDPE pipe can be accredited to various corrugation growth, or

| Table 2 Equations for Comparing Relative Pipe Sizes |  |  |
| :---: | :---: | :---: |
|  | Comparative Diameter to Concrete Pipe |  |
|  | Mannings $\boldsymbol{n}$ for Concrete Pipe |  |
| HDPE Pipe | $n=0.012$ | $n=0.013$ |
| $n=0.012$ | $\mathrm{D}_{\mathrm{p}}=1.000 \mathrm{D}_{\mathrm{c}}$ | $\mathrm{D}_{\mathrm{p}}=0.970 \mathrm{D}_{\mathrm{c}}$ |
| $n=0.024$ | $\mathrm{D}_{\mathrm{p}}=1.297 \mathrm{D}_{\mathrm{c}}$ | $\mathrm{D}_{\mathrm{p}}=1.258 \mathrm{D}_{\mathrm{c}}$ |
| Corrugated Metal Pipe |  |  |
| $n=0.029$ | $\mathrm{D}_{\mathrm{m}}=1.392 \mathrm{D}$ c | $\mathrm{D}_{\mathrm{m}}=1.351 \mathrm{D}_{\mathrm{c}}$ |
| $n=0.034$ | $\mathrm{D}_{\mathrm{m}}=1.478 \mathrm{D}_{\mathrm{c}}$ | $\mathrm{D}_{\mathrm{m}}=1.434 \mathrm{D}_{\mathrm{c}}$ |
| Spiral Rib Metal Pipe |  |  |
| $n=0.016$ | $\mathrm{D}_{\mathrm{m}}=1.114 \mathrm{D}_{\mathrm{c}}$ | $\mathrm{D}_{\mathrm{m}}=1.081 \mathrm{D}_{\mathrm{c}}$ |
| $n=0.018$ | $\mathrm{D}_{\mathrm{m}}=1.164 \mathrm{D}_{\mathrm{c}}$ | $\mathrm{D}_{\mathrm{m}}=1.130 \mathrm{D}_{\mathrm{c}}$ |

waviness, in the liner. The design values shown for HDPE pipe have also allowed for additional corrugation growth once load is applied in the installed condition. The variation found in Corrugated Metal Pipe is dependent on the specified corrugation size from $2-2 / 3^{\prime \prime} \times 1 / 2^{\prime \prime}$ up to a 3 " x $1^{\prime \prime}$ corrugation. All of the listed pipe materials have been tested at the Utah State University Water Research Laboratory. These laboratory values are from those test results. The concrete pipe test reports are available from ACPA's Resources. Contact ACPA or your local concrete pipe supplier for copies of specific reports.

Substituting the recommended $n$ values in the equation for comparing flow capacities of concrete and other smooth-walled pipe with the three available corrugation patterns of corrugated metal pipe, results in the equations in Table 2. $D_{c}$ is the diameter of concrete and other smooth walled pipe and Dm the diameter of corrugated metal pipe.

Tables 3 and 4 have been prepared for direct comparison of required corrugated metal pipe sizes to assure that the hydraulic capacity is at least equivalent to concrete or other smooth-walled pipe.

## EXAMPLE

Given: A 42-inch diameter concrete pipe with a Manning $n$ value of 0.012 flowing full on a given slope.

Find: Size of corrugated metal pipe, HDPE, and spiral rib pipe required to carry the same flow on the same slope as the 42 -inch diameter concrete pipe.

## Solution:

| Type of Pipe | Size from |
| :--- | :---: |
| Concrete | 42 |
| HDPE $(n=0.12)$ | 42 |
| HDPE $(n=0.024)$ | 54 |
| CMP $(n=0.029)$ | 60 |
| CMP $(n=0.034)$ | 66 |
| Spiral Rib $(n=0.016)$ | 48 |
| Spiral Rib $(n=0.018)$ | 54 |

Table 3 Equivalent Flow Capacities Using Available Pipe Sizes, $\mathrm{n}_{\mathrm{c}}=\mathbf{0 . 0 1 2}$

| Concrete <br> Pipe Diameter | HDPE <br> Pipe Diameter |  | Corrugated Metal Pipe <br> Diameter |  | Spiral Rib Metal Pipe <br> Diameter |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{n}=0.012$ | $\mathrm{n}=0.012$ | $\mathrm{n}=0.024$ | $\mathrm{n}=0.029$ | $\mathrm{n}=0.034$ | $\mathrm{n}=0.016$ | $\mathrm{n}=0.018$ |
| 12 | 12 | 18 | 18 | 18 | 15 | 15 |
| 15 | 15 | 21 | 21 | 24 | 18 | 18 |
| 18 | 18 | 24 | 27 | 27 | 21 | 21 |
| 21 | 21 | 27 | 30 | 33 | 24 | 24 |
| 24 | 24 | 33 | 33 | 36 | 27 | 30 |
| 27 | 27 | 36 | 42 | 42 | 30 | 33 |
| 30 | 30 | 42 | 42 | 48 | 33 | 36 |
| 33 | 33 | 48 | 48 | 54 | 42 | 42 |
| 36 | 36 | 48 | 54 | 54 | 42 | 42 |
| 42 | 42 | 54 | 60 | 66 | 48 | 54 |
| 48 | 48 | 66 | 72 | 72 | 54 | 60 |
| 54 | 54 | 72 | 78 | 84 | 60 | 66 |
| 60 | 60 | 78 | 84 | 90 | 72 | 72 |
| 66 | 66 | 90 | 96 | 102 | 78 | 78 |
| 72 | 72 | 96 | 102 | 108 | 84 | 84 |
| 78 | 78 | 102 | 114 | 120 | 90 | 96 |
| 84 | 84 | 114 | 120 | 126 | 96 | 102 |
| 90 | 90 | 120 | 126 | 138 | 102 | 108 |
| 96 | 96 | 126 | 138 | 144 | 108 | 114 |
| 102 | 102 | 132 | 144 |  | 114 | 120 |
| 108 | 108 | 144 |  |  | 120 | 126 |
| 114 | 114 |  |  |  |  | 132 |
| 120 | 120 |  |  |  |  | 138 |
| 126 | 126 |  |  |  |  | 144 |
| 132 |  |  |  |  |  |  |
| 148 | 138 |  |  |  |  |  |

Table 4 Equivalent Flow Capacities Using Available Pipe Sizes, $\mathrm{n}_{\mathrm{c}}=\mathbf{0 . 0 1 3}$

| Concrete <br> Pipe Diameter | HDPE <br> Pipe Diameter |  | Corrugated Metal <br> Pipe Diameter |  | Spiral Rib Metal <br> Pipe Diameter |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{n}=0.013$ | $\mathrm{n}=0.012$ | $\mathrm{n}=0.024$ | $\mathrm{n}=0.029$ | $\mathrm{n}=0.034$ | $\mathrm{n}=0.016$ | $\mathrm{n}=0.018$ |
| 12 | 12 | 15 | 18 | 18 | 15 | 15 |
| 15 | 15 | 21 | 21 | 23 | 18 | 18 |
| 18 | 18 | 24 | 24 | 27 | 21 | 21 |
| 21 | 21 | 27 | 30 | 30 | 24 | 24 |
| 24 | 24 | 30 | 33 | 33 | 27 | 27 |
| 27 | 27 | 36 | 42 | 42 | 30 | 33 |
| 30 | 30 | 42 | 42 | 48 | 33 | 36 |
| 33 | 33 | 42 | 48 | 48 | 36 | 42 |
| 36 | 36 | 48 | 54 | 54 | 42 | 42 |
| 42 | 42 | 54 | 60 | 60 | 48 | 48 |
| 48 | 48 | 60 | 66 | 72 | 54 | 54 |
| 54 | 54 | 72 | 78 | 78 | 60 | 66 |
| 60 | 60 | 78 | 84 | 90 | 66 | 72 |
| 66 | 66 | 84 | 90 | 96 | 72 | 78 |
| 72 | 72 | 96 | 102 | 108 | 78 | 84 |
| 78 | 78 | 102 | 108 | 114 | 84 | 90 |
| 84 | 84 | 108 | 114 | 120 | 96 | 96 |
| 90 | 90 | 114 | 126 | 132 | 102 | 102 |
| 96 | 96 | 126 | 132 | 138 | 108 | 108 |
| 102 | 102 | 132 | 138 |  | 114 | 120 |
| 108 | 108 | 138 |  |  | 120 | 126 |
| 114 | 114 | 144 |  |  | 126 | 132 |
| 120 | 120 |  |  |  |  | 132 |
| 132 | 132 |  |  |  |  | 144 |
| 138 | 132 | 138 |  |  |  |  |

